



# Full Syllabus



## Course Title

Ordinary Differential Equations 1

## Lecturer

Arie Levant

## Semester

A

## Course requirements

## Final grade components

20% homework (7-10 assignments) + 80% exam

## Course schedule

Class no. / Date	Subject and Requirements (assignments, reading materials, tasks, etc.)
	Notation. Differential (recalling). Classification of differential equations (DEs). 1st order DEs: separable, linear, Bernoulli, homogeneous, exact DE. 1st integral. Integrating factor notion. Change of variables. Systems of DE, Lotka-Volterra system.
	Cauchy problem. Vector fields. Phase space. Methods of Picard and Euler. Lipschitz condition. Theorem of the existence and uniqueness of the solution. Fixed point of a contractive mapping.
	Solution dependence on the initial conditions, the right-hand side and parameters. Solution extension. Autonomous DE. Critical points. Linearization.
	System of 1st order linear DEs. Gronwall-Bellman lemma. Solution space. Fundamental solutions. Linear dependence of functions. Wronskian.
	Systems of 1st order DEs with constant coefficients. Matrix exponent: real and complex eigenvalues, multiplicity. Exponent calculation and solution of homogeneous systems.
	High order scalar linear DEs, homogeneous and non-homogeneous. Quasi-polynomials.
	Non-homogeneous system of 1st order DEs with constant coefficients. Vector quasi-polynomials. Method of undetermined coefficients in scalar and vector cases. Method of coefficient variation. Euler equations. Abel-Liouville theorem: vector, scalar cases. Decreasing the order of DE. Solution of differential equations via power series.
	Dynamic systems, Critical points in plane. Lyapunov stability and Lyapunov functions.

## Required course reading

Notes and other materials will be provided

## Optional course reading

Boyce W.E. and DiPrima R.C. Elementary Differential Equations and Boundary Value Problems  
Arnold V.I. Ordinary Differential Equations

## Comments

The course is taught in English.